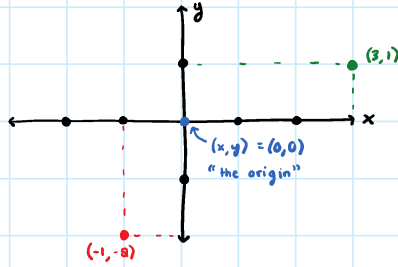


# The Plane

Monday, May 1, 2023 8:51 AM

- real plane : all pairs of real #'s  $(x, y)$
- point : one pair of real #'s / ex)  $(3, 4) = \text{point}$

drawing of plane:



types of questions:

- 1) give equation : draw solutions
- 2) compute quantities : distances, magnitudes, intersections

ex 1) check if points are in  $\{2x - y = 1\}$

- $(0, 0) \times$        $2(0) - 0 = 1 \rightarrow 0 = 1$  (doesn't belong)
- $(0, -1) \checkmark$        $2(0) - (-1) = 1 \rightarrow 1 = 1$  (belongs)
- $(2, 3) \checkmark$        $2(2) - 3 = 1 \rightarrow 1 = 1$  (belongs)

def : a line is any set in plane given by equation of form:

infinite

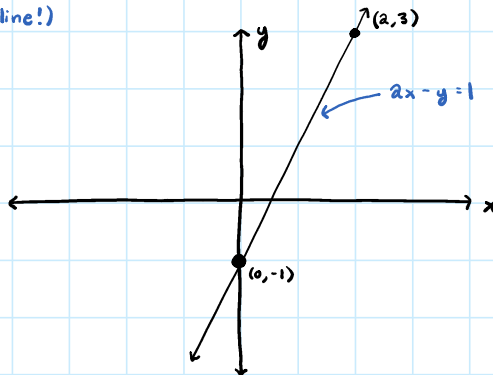
$$\underline{ax + by = d}$$

\* anything but plain  $x$  &  $y \neq$  line / parabola, hyperbola, circle etc.  $\neq$  line \*

previous ex)  $a = 2$     $b = -1$     $d = 1$

ex 1 cont) draw  $\{2x - y = 1\}$  (a line!)

- plug in values for  $x \rightarrow$  get  $y$
- line / circle = need 2 points
- plane = need 3 points



\* if  $d = 0$ , then line goes thru origin / not in this ex \*

how to draw solutions of equations?

- 1) sample points (check if equation holds for values given)
- 2) use knowledge on equations (lines, circles)

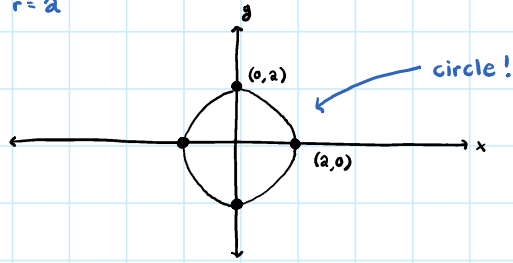
ex 2) draw  $\{x^2 + y^2 = 4\} \rightarrow r=2$   
(not line  $\rightarrow$  circle)

(0,0) x

(2,0) ✓

(0,2) ✓

(1,1) x



def: a circle of radius  $r$  centered @  $(0,0)$  is given by equation:

$$\underline{x^2 + y^2 = r^2}$$

previous ex)  $r=2$

#'s in front of  $x$  &  $y$  could be circle or not / depends

